

Quantum memory for entangled continuous-variable states

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A quantum memory for light is a key element for the realization of future quantum information networks^{1–3}. Requirements for a good quantum memory are versatility (allowing a wide range of inputs) and preservation of quantum information in a way unattainable with any classical memory device. Here we demonstrate such a quantum memory for continuous-variable entangled states, which play a fundamental role in quantum information processing^{4–6}. We store an extensive alphabet of two-mode 6.0 dB squeezed states obtained by varying the orientation of squeezing and the displacement of the states. The two components of the entangled state are stored in two room-temperature cells separated by 0.5 m, one for each mode, with a memory time of 1 ms. The true quantum character of the memory is rigorously proved by showing that the experimental memory fidelity 0.52 ± 0.02 significantly exceeds the benchmark of 0.45 for the best possible classical memory for a range of displacements.

The continuous-variable regime represents one of the principal avenues towards the realization of quantum information processing and communication^{4–6}. In the optical domain it operates with well-known optical modulation and detection techniques and allows for deterministic quantum operations. In the atomic domain it has been developed on the platform of atomic ensembles^{2,3,7}. Advances in the realization of continuous-variable quantum protocols include unconditional quantum teleportation involving light⁸ and atoms⁹, a number of results on memory^{2,3,10,11} and quantum key distribution¹². Hybrid continuous/discrete-variable operations^{13–15} paving the road towards continuous-variable quantum computation^{16,17} have also been reported. However, the ability to store non-classical continuous-variable states of light is crucial to enable further progress, in particular, for continuous-variable linear optics quantum computing with offline resources¹⁷, continuous-variable quantum repeaters^{18,19}, entanglement-enhanced quantum metrology, iterative continuous-variable entanglement distillation²⁰, continuous-variable cluster-state quantum computation²¹, communication/cryptography protocols involving several rounds²² and quantum illumination²³. Compared with a number of impressive results reporting discrete-variable quantum memories at the single-photon level (see reviews^{1–3} and references therein), there have been very few experiments towards quantum memory for continuous-variable non-classical states. A fractional, 20 nsec, delay of 50 nsec pulsed continuous-variable entangled states in the atomic

vapour has recently been demonstrated²⁴. Memory based on electromagnetically induced transparency for a squeezed vacuum state has been reported^{25,26}, albeit with the fidelity below the classical benchmark²⁷. Very recently, classical benchmarks for storing displaced squeezed states^{28,29} have been derived, which made experimental implementation of such storage a timely challenge. Such states form an alphabet for continuous-variable quantum information encoding¹⁶. An exciting feature of displaced squeezed states is that the ratio of the quantum to classical fidelity grows inversely proportionally to the degree of squeezing.

Here we report the realization of a quantum memory for a set of displaced two-mode squeezed states with an unconditionally high fidelity that exceeds the classical benchmark calculated on the basis of the method in ref. 28. The fidelity between the input state and the memory state is a sufficient condition for a memory or a teleportation protocol to be genuinely quantum. In fact, because continuous-variable protocols are deterministic, that is they have a unity efficiency, the fidelity becomes the preferred performance criterion. The experimental fidelity demonstrated here, which exceeds the classical benchmark fidelity, implies that our quantum memory cannot be mimicked by any classical device.

We store a displaced entangled state of two sideband modes of light \hat{a}_+ and \hat{a}_- with the frequencies $\omega_{\pm} = \omega_0 \pm \omega_L$, where ω_0 is the carrier frequency of light. The entanglement condition for this Einstein–Podolsky–Rosen state⁶ is $\text{Var}(\hat{X}_+ + \hat{X}_-) + \text{Var}(\hat{P}_+ - \hat{P}_-) < 2$ (ref. 30) where canonical quadrature operators obey $[\hat{X}_{\pm}, \hat{P}_{\pm}] = i$. For a vacuum state $\text{Var}(\hat{X}_{\text{vac}}) = \text{Var}(\hat{P}_{\text{vac}}) = 1/2$. The entanglement of the \hat{a}_+ and \hat{a}_- modes is equivalent to simultaneous squeezing of the $\cos(\omega_L t)$ mode $\hat{x}_{Lc} = (\hat{X}_+ + \hat{X}_-)/\sqrt{2}$; $\hat{p}_{Lc} = (\hat{P}_+ + \hat{P}_-)/\sqrt{2}$ and the corresponding $\sin(\omega_L t)$ mode. Before the input state of light undergoes various losses it is a 6 dB squeezed state. In the photon-number representation for the two modes, the state is $|\Psi\rangle = 0.8|0\rangle_+|0\rangle_- + 0.48|1\rangle_+|1\rangle_- + 0.29|2\rangle_+|2\rangle_- + 0.18|3\rangle_+|3\rangle_- + \dots$. The displaced squeezed states are produced (Fig. 1a) using an optical parametric amplifier³¹ (OPA) with the bandwidth of 8.3 MHz and two electro-optical modulators (EOMs; see the Methods section for details). The alphabet of quantum states Ψ_i , which we refer to as ‘initial pure states’ (see the inset in Fig. 2 and Table 1) is generated by displacing the two-mode squeezed vacuum state by varying values $[\langle x_{Lc} \rangle; \langle p_{Lc} \rangle] = [0, 3.8, 7.6; 0, 3.8, 7.6]$

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Table 1 | Initial states of light and stored memory states.

Initial states Ψ_i			Stored states				Overlap
$\langle x_L \rangle$	$\langle p_L \rangle$	ϕ	$\langle p_A^{\text{fin}} \rangle$	$\langle x_A^{\text{fin}} \rangle$	$\text{Var}(p_A^{\text{fin}})$	$\text{Var}(x_A^{\text{fin}})$	Θ_i
0.0	0.0	0	-0.06	0.25	0.52(2)	1.99(3)	0.62
0.0	3.8		-0.06	3.19			0.60
3.8	0.0		-3.47	-0.42			0.57
3.8	3.8		-3.39	2.89			0.49
0.0	0.0	90	-0.07	0.06	1.95(6)	0.73(1)	0.55
0.0	3.8		-0.06	3.14			0.42
3.8	0.0		-3.22	0.48			0.46
3.8	3.8		-3.21	3.59			0.50
0.0	7.6	0	-0.03	6.30	0.55(2)	2.01(4)	0.49
7.6	0.0		-6.83	-0.46			0.37
3.8	7.6		-3.20	6.07			0.35
7.6	3.8		-6.54	2.80			0.22
7.6	7.6		-6.40	6.03			0.15
0.0	7.6	90	-0.08	6.24	2.12(8)	0.78(3)	0.18
7.6	0.0		-6.37	0.59			0.35
3.8	7.6		-3.13	6.75			0.32
7.6	3.8		-6.38	3.79			0.43
7.6	7.6		-6.36	6.72			0.27

The three first columns show the mean displacements and the squeezing phase ($\phi = 0$ corresponds to x_L being squeezed) of the initial pure light states. The next four columns show the mean values and variances of the atomic states after the storage. The last column shows the overlap between the initial pure light states and the stored atomic states. Vacuum-state variances are 0.5. The uncertainties on the variances are calculated as the standard deviation of the variances within each subgroup of the input states.

feedback into both the c and s modes. The feedback is achieved with pulses of the magnetic field at the frequency ω_L applied to the two cells. The memory input light pulse is then sent, followed by the measurement of the output light operator x_L' by the polarization homodyne detection. The measurement result is fed back onto the p_A' with a gain g . The resulting x_A^{fin} and p_A^{fin} for the optimized g and $\kappa = 1$ can be found from equation (1)

$$x_A^{\text{fin}} = \sqrt{1 - \frac{1}{Z^2}} x_A + p_L \quad \text{and} \quad p_A^{\text{fin}} = -x_L \quad (2)$$

In the absence of decoherence the operator x_L is perfectly mapped on the memory operator p_A^{fin} . The operator p_L is stored in x_A^{fin} with the correct mean value $\langle p_L \rangle = \langle x_A^{\text{fin}} \rangle$ (as $\langle x_A \rangle = 0$) but with an additional noise due to x_A .

The ability to reproduce the correct mean values of the input state in the memory by adjusting g and κ is a characteristic feature of our protocol that arguably makes it better suited for storage of multiphoton states compared with, for example, electromagnetically induced transparency and photon-echo approaches where such an adjustment, to the best of our knowledge, has not been demonstrated.

The deleterious noise of the initial state of atoms x_A is suppressed by the initial spin-squeezing sequence and by the extra factor $\sqrt{1 - 1/Z^2} = 0.92$ due to the swap interaction. In the absence of passive (reflection) losses for light and atomic decoherence we find from equation (2) the expected fidelity of 0.95 and 0.61 for the states squeezed with the $\phi = 0^0$ and $\phi = 90^0$, respectively, with the mean fidelity of 0.78.

The true quantum character of our memory is preserved despite substantial transmission losses schematically shown in the bottom of Fig. 2. Entangled states of light are sent to the receiver memory station through a channel with the transmission coefficient $\eta_{\text{tr}} = 0.80(4)$ (which includes the OPA output coupling efficiency 0.97) resulting in the ‘memory input

state’, ρ_{in} , with $\text{Var}(x_L \cdot \cos(\phi) - p_L \cdot \sin(\phi)) = 0.20(2)$ and $\text{Var}(x_L \cdot \sin(\phi) + p_L \cdot \cos(\phi)) = 1.68(9)$. The entrance (reflection) losses at the windows of the memory cells lead to further attenuation by the factor $\eta_{\text{ent}} = 0.90(1)$. Between the interaction and detection light experiences losses described by the detection efficiency $\eta_{\text{det}} = 0.79(2)$ (see the Methods section).

Following the storage time of 1 ms between the end of the input pulse and the beginning of the verifying pulse (see Fig. 1b for the time sequence) we measure the atomic operators with a verifying probe pulse. The measured mean values and variances of the atomic operators x_A^{fin} and p_A^{fin} are summarized in Table 1 (see the Methods section for calibration of the atomic operators). From these values and the loss parameters, we can calculate the noise added during the storage process that comes on top of the noise added by transmission and entrance losses. We find that the memory adds 0.47 (6) to $\text{Var}(x_A^{\text{fin}})$ and 0.38 (11) to $\text{Var}(p_A^{\text{fin}})$, whereas for the ideal memory, according to equation (2), we expect the additional noise to be 0.36 (5) (due to the finite squeezing of the initial atomic operator x_A) and 0, for the two quadratures, respectively. This added noise can be due to atomic decoherence, uncanceled noise from the initial antisqueezed p_A quadrature and technical noise from the EOMs.

The overlap integrals between the stored states and the initial pure states are given in the Table 1. The average fidelities calculated from the overlap values for square input distributions with the size $d_{\text{max}} = 0, 3.8$ and 7.6 are plotted in Fig. 2. The choice of the interaction strength $\kappa = 1$ minimizes the added noise but leads to the mismatch between the mean values of the stored atomic state and of the initial pure state of light by the factor $\sqrt{\eta_{\text{ent}} \cdot \eta_{\text{tr}}} = 0.85$. This mismatch is the reason for the reduction of the experimental fidelity for states with larger displacements.

The classical benchmark memory fidelity is calculated²⁸ from the overlap of displaced Ψ_i states with the states stored in the (hypothetical) classical memory positioned in place of the quantum memory (see the panel in the bottom of Fig. 2). This ensures that the classical memory has the same input state ρ_{in} as the quantum memory that is Ψ_i propagated through the transmission channel with $\eta_{\text{tr}} = 0.80$. The benchmark fidelity is found as an average overlap for an input distribution within a square $\{|\langle x_L \rangle|, |\langle p_L \rangle| \leq d_{\text{max}}\}$ with all input states with the mean values within the square having equal probability. The squeezing of the pure input states is fixed to the experimental value of 6 dB, and all phases of squeezing are allowed. The upper bound values on the classical benchmark fidelity are plotted in Fig. 2. The benchmark values have been obtained by first truncating the Hilbert space to a finite photon number and then solving the finite-dimensional optimization employing semi-definite programming. The result of the truncation of the Hilbert space is the constant upper bound of 0.45 of the benchmark for $d_{\text{max}} > 3.5$ (see Supplementary Information), whereas the actual benchmark decreases further for a larger d_{max} (the benchmark for an infinite Gaussian distribution²⁸ of displacements is 0.38).

For the experimental alphabet with $d_{\text{max}} = 3.8$ the experimental fidelity (the average overlap integral for the top eight representative states in Table 1) is higher than the classical benchmark value, which proves the true quantum nature of the memory.

Outperforming the classical benchmark means that our memory is capable of preserving entanglement in the case when one of the two entangled modes is stored whereas the other is left propagating, which is the case, for example, in the quantum repeater. Using experimentally obtained values of the added noise we evaluate the performance of our memory for the protocol where the upper sideband \hat{a}_+ mode is stored in one of the memory cells whereas the other entangled mode \hat{a}_- is left as a propagating light mode. We find the Einstein–Podolsky–Rosen variance between the stored mode and the propagating mode to be 1.52 (−1.2 dB below the

separability criterion), which corresponds to the lower bound on the entanglement of formation of $\sim 1/7$ ebit (see Supplementary Information for details of the calculation). This version of the memory can be implemented by splitting the \hat{a}_- and \hat{a}_+ modes, which can be accomplished by a narrow-band optical cavity.

We have experimentally demonstrated the deterministic quantum memory for continuous-variable multiphoton entangled states. The present memory lifetime is limited by collisions and residual magnetic fields leading to the decoherence time of 30 ms. The fidelity can be further improved by means of reduction of the reflection losses, increasing the initial atomic spin squeezing and reduction of the atomic decoherence. Our approach is feasible also for non-Gaussian continuous-variable multiphoton states. Stored states can be directly processed in the atomic memory, as in the repeater scheme¹⁸, measured, as in multi-round protocols²², or transferred onto another processor by means of teleportation³.

Methods

Verification. Atomic memory state tomography is carried out by measuring the x_L' of the verification pulse equation (1). We run a series of measurements of p_A^{fin} and x_A^{fin} , the latter carried out after applying a magnetic π -pulse before the verification pulse, for many copies of the same input state of light. Owing to the Gaussian statistics of the states, the mean values and the variances of x_A^{fin} and p_A^{fin} are sufficient for a complete description of the atomic state.

Calibrations. Before carrying out the storage, we calibrate the interaction strength κ and the feedback gain g , such that the mean values of the light state inside the memory (that is, after the entrance loss) are transferred faithfully. κ is calibrated by creating a mean value $\langle p_L^{\text{input}} \rangle$ in the input pulse. The mean is stored in the atomic x_A' , which is read out after the magnetic π -pulse with the probe pulse. The measured mean of the probe pulse is then $\langle x_L^{\text{probe}} \rangle = \kappa^2 \langle p_L^{\text{input}} \rangle$, from which κ^2 is determined. Using similar methods we can calibrate the electronic feedback gain g .

Generation of the displaced squeezed input states. The OPA, which is pumped by the second harmonic of the master laser and generates the entangled squeezed vacuum states, is seeded with a few microwatts of the master laser light with the carrier frequency ω_0 , which is amplitude and phase modulated by two EOMs at a frequency of 322 kHz, thus creating coherent states in the ± 322 kHz sidebands around ω_0 (Fig. 1). With such a modulated seed, the output of the OPA is a displaced two-mode squeezed state. The output of the OPA is mixed at a polarizing beam splitter with the strong local oscillator (driving) field from the master laser.

Losses. To calculate the mean values and variances of the stored state and the input states, we need to know the optical losses. The total losses η_{tot} can be divided into three parts, the channel propagation transmission η_{tr} from the OPA to the front of the memory cells (including the OPA output efficiency of 0.97), the entrance transmission η_{ent} and the detection efficiency η_{det} , such that $\eta_{\text{tot}} = \eta_{\text{tr}} \cdot \eta_{\text{ent}} \cdot \eta_{\text{det}}$ (all of the η terms are intensity transmission coefficients). From the measurement of the quadratures of the squeezed light (with variances 0.29 (1) and 1.34 (6)), we find the total losses $\eta_{\text{tot}} = 0.567(35)$. We measure the transmission through the cells of 0.817 (20), the transmission through the optics after the cells of 0.889 (10) and estimate the efficiency of the photodiodes to be 0.98 (1). Assigning one-half of the losses through the cells to the entrance losses and the other half to the detection losses we find $\eta_{\text{ent}} = \sqrt{0.817} = 0.90(1)$, $\eta_{\text{det}} = \sqrt{0.817} \cdot 0.889 \cdot 0.98 = 0.79(2)$ and $\eta_{\text{tr}} = \eta_{\text{tot}} / (\eta_{\text{ent}} \eta_{\text{det}}) = 0.80(4)$.

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Additional information

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